

Problem 1

Given two hot and two cold streams with the following data:

Name	Type	T_s °C	T_t °C	Q kW
H1	Hot	250	40	31500
H2	Hot	200	80	30000
C1	Cold	20	180	32000
C2	Cold	140	230	27000

- Calculate the CP (kW/K) for each stream.
- The minimum temperature difference in this process is set to 10°C. Draw composite curves for the hot and cold streams such that $\Delta T_{\min} = 10^\circ\text{C}$.
- What is minimum demand for external heating and cooling and what is maximum heat recovery?
- Use the rules for design of heat exchanger networks (pinch design rules) and draw a network that may give maximum heat recovery.

a) Ved at $Q = C_p \Delta T \Rightarrow C_p = \frac{Q}{\Delta T}$

Dermed: $C_{p,H1} = 150 \text{ kW/K}$

$C_{p,H2} = 250 \text{ kW/K}$

$C_{p,C1} = 200 \text{ kW/K}$

$C_{p,C2} = 300 \text{ kW/K}$

b)

Stream	$C_p \text{ [kW/K]}$	$T_s - T_t$	$\Delta H/Q$	$T'_s - T'_t$
H ₁	150	250-40	31500	245-35
H ₂	250	200-80	30000	195-75
C ₁	200	20-180	32000	25-185
C ₂	300	140-230	27000	145-235

Hot composite curve:

$\Delta T'$	Streams	Energy
245-195	H ₁	7500
195-75	H ₁ + H ₂	48000
75-35	H ₁	6000

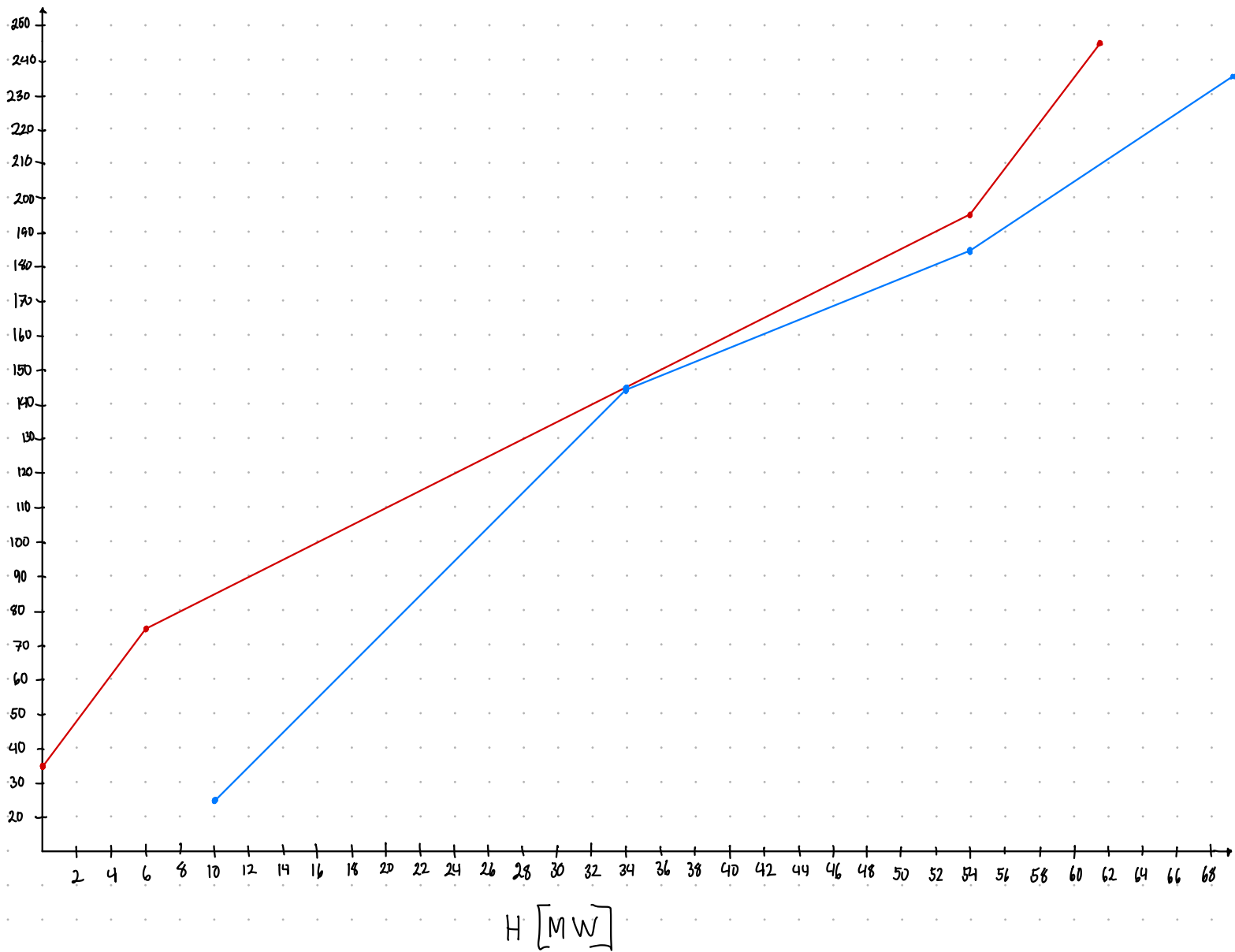
Cold composite curve

$\Delta T'$	Streams	Energy
25-145	C ₁	24000
145-185	C ₁ + C ₂	20000
185-235	C ₂	15000

From problem tabel (Jørgensen ned), pinch ved 145°C

Da her $H_{\text{varm}} = 6000 + (150+250) \cdot (145-75) = 34000$

$\Rightarrow$ Starb $H_{\text{kold p}} = 34000 - 24000 = 10000$



c)

Problem tabell:

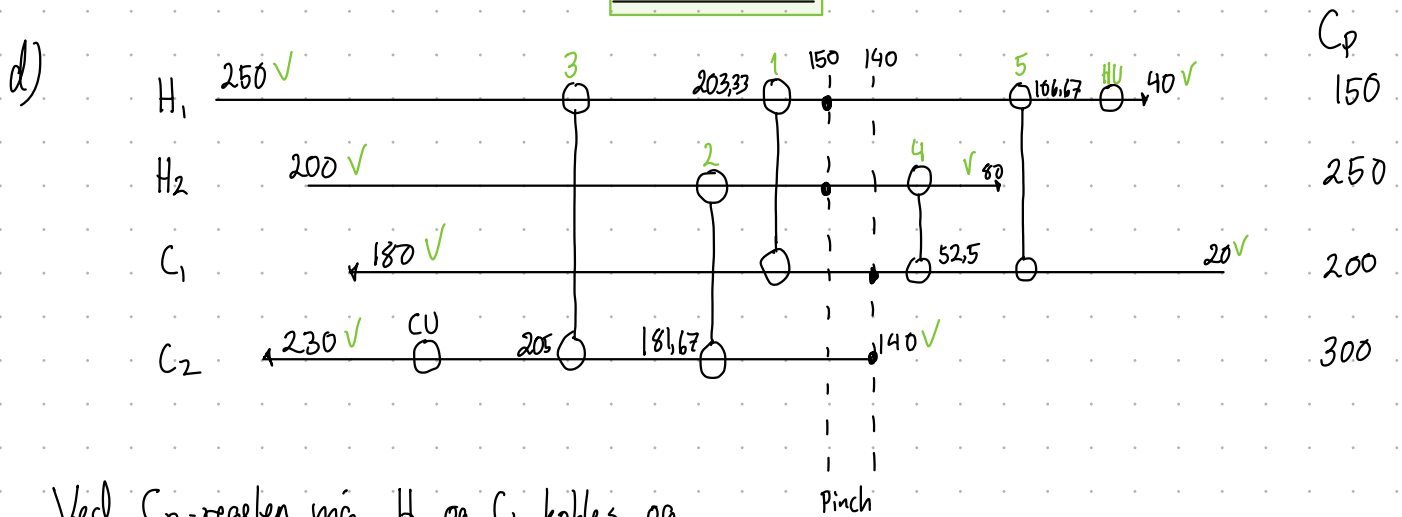
		$[\sum C_{p,h} - \sum C_{p,c}] \Delta T$		
T'	Strøm	ΔH	$ST=0$	$ST=7500$
245	H_1	+1500	0	7500
235	H_1	-6000	1500	9000
195	H_1, H_2	+1000	-4500	3000
185	H_1, H_2, C_1, C_2	-4000	-3500	4000
145	H_1, H_2, C_1	+14000	-7500	0 Pinch
75	H_1, C_1	-2000	6500	14000
35	C_1	-2000	4500	12000
25			2500	10000

Ser fra tabellen • at minimum ekstern oppvarming er 7500 kW
minimum ekstern kjøling er 10 000 kW

$$Q_{rec} = \sum \Delta H_H - Q_{c,min}$$

$$= 61500 - 10000$$

$$= \underline{\underline{51500 \text{ kW}}}$$



Ved C_p -regelen må H_1 og C_1 kobles, og

H_2 og C_2 ved pinch varmeveksler

HX1: $H_1: (250 - 150) \cdot 150 = 15000$

$C_1: (180 - 140) \cdot 200 = 8000$

} C_1 blir "tømt"

$$T_{H1, ut} = 150 + \frac{8000}{150} = 203,33$$

HX2: $H_2: (200 - 150) \cdot 250 = 12500$

$C_2: (230 - 140) \cdot 300 = 27000$

} H_2 ferdig

$$T_{C2, ut} = 140 + \frac{12500}{300} = 181,67$$

Henner ut restende varme i H_1 ved HX3

HX3: $H_1: (250 - 203,33) \cdot 150 = 7000$

$C_2: (230 - 181,67) \cdot 300 = 14500$

} H_1 ferdig

$$T_{C2, ut} = 181,67 + \frac{7000}{300} = 205 \Rightarrow \Delta T_{min} \text{ er bevert i HX3}$$

CU: $Q_u = 14500 - 7000 = 7500 \Rightarrow$ Stemmer med c)

Under pinch : $C_{p,c} \leq C_{p,h}$

Køler H_2 og C_1

$$\text{HX4: } \left. \begin{array}{l} H_2 : (150 - 80) \cdot 250 = 17500 \\ C_1 : (140 - 20) \cdot 200 = 24000 \end{array} \right\} H_2 \text{ ferdig}$$

$$T_{C1, ut} = 140 - \frac{17500}{200} = 52,5$$

Kjøler ned H_1 med "resten" av C_1

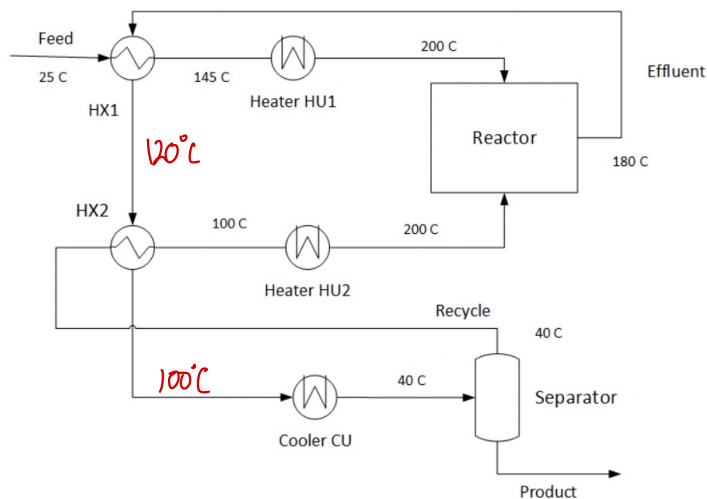
$$\text{HX5: } \left. \begin{array}{l} H_1 : (150 - 40) \cdot 150 = 16500 \\ C_1 : (52,5 - 20) \cdot 300 = 6500 \end{array} \right\} C_1 \text{ "færdig"}$$

$$T_{H1, ut} = 150 - \frac{6500}{150} = 106,67 \Rightarrow \Delta T_{min} \text{ er opprettholdt.}$$

$$\text{HU: } Q_h = 16500 - 6500 = 10000 \text{ som stemmer med oppgave c)}$$

Problem 2

An existing process is as described in the figure below.



For the existing design:

- Calculate the temperature of the effluent stream after the two heat exchangers, HX1 and HX2
- Calculate the duty of the two heaters and the cooler
- Calculate the necessary area of the second heat exchanger (HX2) when the overall heat transfer is $100 \text{ W/(m}^2\text{K)}$

The existing process may not be a maximum energy recovery design.

- Calculate the minimum external heating and cooling when the minimum temperature approach between cold and hot streams is 10°C and find the pinch temperature
- If the existing process is not a maximum energy recovery design, make a new design of the heat exchanger network that obtain maximum energy recovery
- Is it possible to reduce the number of heat exchangers? Draw the new design similar to the figure above

The start and target temperatures of the three streams are as indicated in the figure and data are given in the table below.

Stream	Start temperature $[\text{C}]$	Target temperature $[\text{C}]$	Overall heat capacity $[\text{kW}/^\circ\text{C}]$
Feed	25	200	3
Effluent	180	40	6
Recycle	40	200	2

a) Assuming no heat loss, $Q_h = Q_c$

$$\text{HX1: } (180 - T) \cdot 6 = (145 - 25) \cdot 3$$

$$\Rightarrow T = 120^\circ\text{C}$$

$$\text{HX2: } (120 - T) \cdot 6 = (100 - 40) \cdot 2$$

$$\Rightarrow T = 100^\circ\text{C}$$

b)

$$Q_{HU1} = (200 - 145) \cdot 3 = 165$$

$$Q_{HU2} = (200 - 100) \cdot 2 = 200$$

$$Q_{CU} = (100 - 40) \cdot 6 = 360$$

c)

$$Q = UA \cdot \Delta T_{lm}$$

$$A = \frac{Q}{\Delta T_{lm}}$$

HX1:

$$Q = 360 \text{ kW}$$

Antar motström

$$\Delta T_1 = 160 - 145 = 35$$

$$\Delta T_2 = 120 - 25 = 95$$

$$\Delta T_{lm} = \frac{\Delta T_2 - \Delta T_1}{\ln \frac{\Delta T_2}{\Delta T_1}} = 60,088 \text{ K}$$

$$A = \frac{360 \cdot 10^3 \text{ W}}{60,088 \text{ K} \cdot 100 \text{ W/m}^2 \text{ K}} = \underline{59,91 \text{ m}^2}$$

HX2:

$$Q = 120 \text{ kW}$$

Antar motström

$$\Delta T_1 = 120 - 100 = 20$$

$$\Delta T_2 = 100 - 40 = 60$$

$$\Delta T_{lm} = \frac{\Delta T_2 - \Delta T_1}{\ln \frac{\Delta T_2}{\Delta T_1}} = 36,410 \text{ K}$$

$$A = \frac{120 \cdot 10^3 \text{ W}}{36,410 \text{ K} \cdot 100 \text{ W/m}^2 \text{ K}} = \underline{32,96 \text{ m}^2}$$

d)

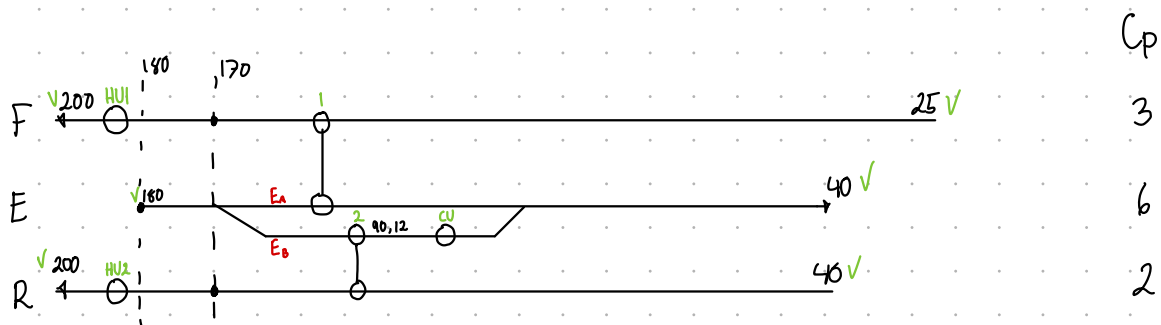
Strøm	$C_p \text{ [kW/K]}$	$T_s - T_t$	$T'_s - T'_t$	$T' = T \pm \frac{1}{2} \Delta T_{lm}$
Feed (F)	3	25 - 200	30 - 205	
Effluent (E)	6	180 - 40	175 - 35	
Recycle (R)	2	40 - 200	45 - 205	

T'	Strøm	$\Delta H = (\sum C_{ph} - \sum C_{pc}) \Delta T$	ST=0	ST=150
205			0	150
176	F R	-150	-150	0 <i>Pinch</i>
45	FE R	+130	-20	130
35	FE	+30	10	160
30	F	-15	-5	145

Fra tabellen: $Q_{h,min} = 150$
 $Q_{c,min} = 145$

Pinch temperature $T' = 176 \Rightarrow \text{Pinch} = 180 - 170$

e) Ser at $Q_{h,min} < Q_{HU1} + Q_{HU2}$ og $Q_{c,min} < Q_{CU} \Rightarrow$ Ikke MER



Over pinch

Har ingen varm strøm å bruke $\Rightarrow$ kun ekstern oppvarming

$$HU1: Q = (200 - 170) \cdot 3 = 90$$

$$HU2: Q = (200 - 170) \cdot 2 = 60$$

Tot: $Q_h = 150$, hvilket er lik $Q_{h,min}$

Under pinch

For å opprettholde ΔT_{min} , må vi splitte E i 2

Antar at vi har splittet slik at E_A "fullfører" F
Dermed

$$\left. \begin{aligned} \text{HX1: } F &: (170 - 25) \cdot 3 = 435 \\ E_A &: (180 - 40) C_{PE_A} = 435 \end{aligned} \right\} F + E_A \text{ ferdig}$$

$$\Rightarrow C_{PE_A} = \frac{435}{180 - 40} = 3,107$$

$$C_{PE_B} = 6 - C_{PE_A} = 2,893$$

$\frac{81}{28}$

$$\left. \begin{aligned} \text{HX2: } E_B &: (180 - 40) \cdot 2,893 = 405 \\ R &: (170 - 40) \cdot 2 = 260 \end{aligned} \right\} R \text{ er ferdig}$$

$$T_{E_B, ut} = 180 - \frac{260}{2,893} = 90,12$$

$$CU: Q_c = 405 - 260 = 145, \text{ stemmer med } Q_{c,min}$$

f) För samma antall varnerekskare

